On Interpolation in Hardy- Orlicz spaces

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Abstract:

The Hardy-Orlicz space H_{ϕ} is the space of all analytic functions f on the open unit disk D such that the subharmonic function $\phi(|f|)$ has a harmonic majorant on D where ϕ is a modulus function.

 H_{ϕ}^{+} is the subspace of H_{ϕ} consisting of all $f \in H_{\phi}$ such that $\phi(|f|)$ has a quasi-bounded harmonic majorant on D. If $\phi(x) = x^{p}, 0 , then <math>H_{\phi}$ is the Hardy space H^{p} and if $\phi(x) = \log(1+x)$, then H_{ϕ} is the Nevanlinna class N and H_{ϕ}^{+} is the Smirnov class N^{+} . In this paper we generalize some of N. Yanagihara's and A. Hartmann's and others interpolation results from N and N^{+} to H_{ϕ} and H_{ϕ}^{+} . For that purpose we generalize a canonical factorization theorem to functions in H_{ϕ} or H_{ϕ}^{+} and introduce an F-space of complex sequences.